

**Infrastructure Commission (INFCOM)**

**Standing Committee on Measurements, Instrumentation and Traceability (SC-MINT)**

**Expert Team on Quality, Traceability and Calibration (ET-QTC)**

# **Calibration of Precipitation Instruments**

## **Part-3: Calibration Examples (1)**

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# Content

## Part 1:

- Introduction to this unit and historical information
- Concepts and definitions

## Part 2:

- Methods of measurement
- Calibration of rain gauges

## Part 3:

- **Calibration example #1**
- Calibration example #2

## Part 4:

- Calibration example #3
- Calibration example #4
- References and links

# Calibration of rain gauges – example #1 (DWD)

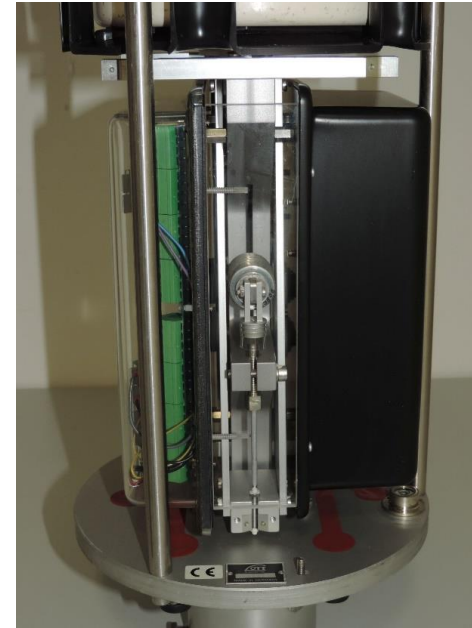
- collecting rain gauge using a weighing unit
  - this rain gauge collects the rain with a container
  - the container is weighed together with the collected rain
  - digital readout of amount and intensity



assembled rain gauge



with housing removed



detailed view of the  
weighing unit

# Calibration of rain gauges – example #1

- the container is removed and a plate with a spindle is placed on top for centring
- instead of water, specially made weights with a hole are placed on the plate



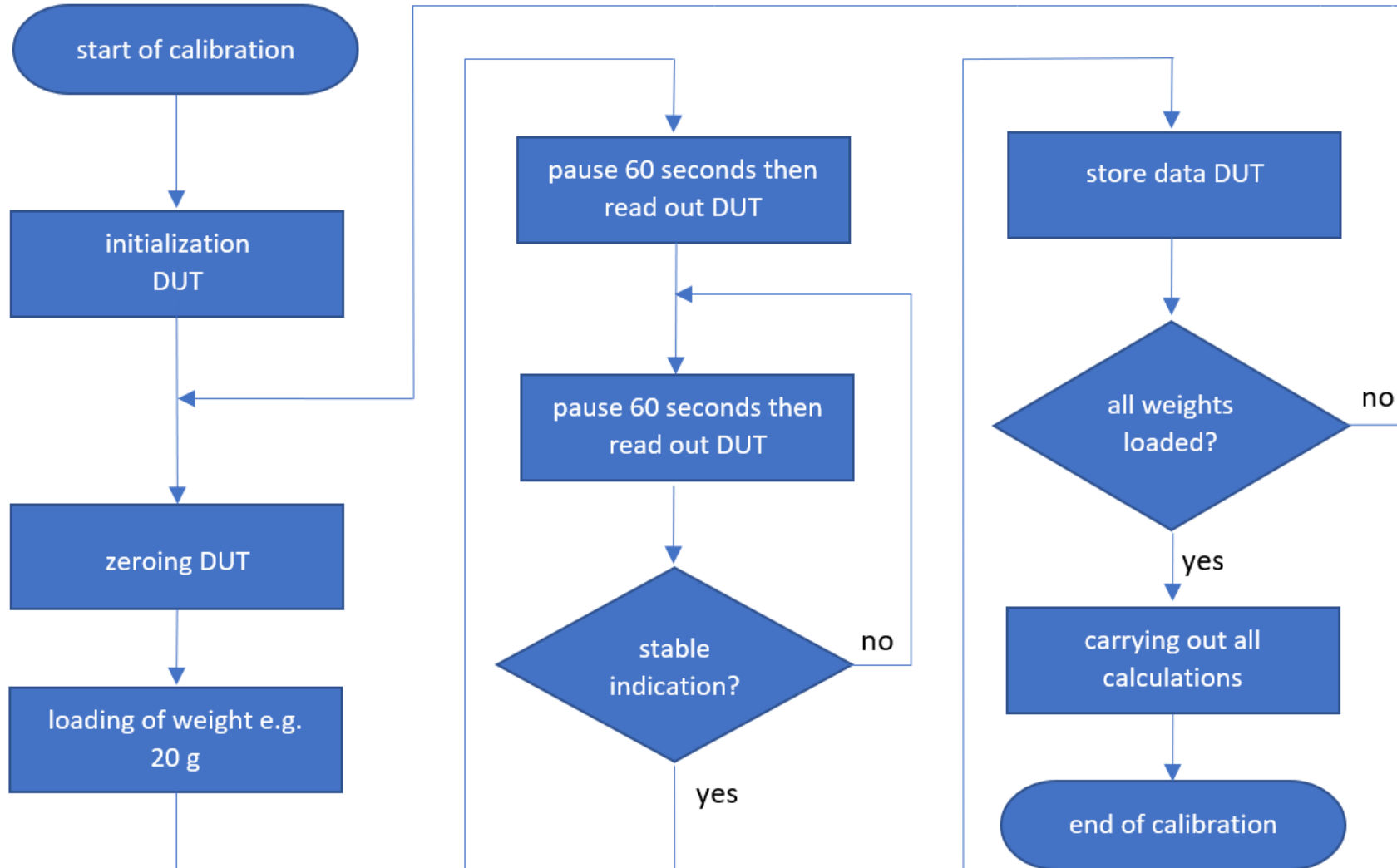
set of weights



loaded weights

- the weights make it possible to simulate the intensity of the rain and the accumulated rain

# Calibration of rain gauges – example #1



# Calibration of rain gauges – example #1

- type A uncertainties
  - due to the very long stabilization times, repetitions are not possible
  - therefore, no type A measurement uncertainties are taken into account
- type B uncertainties
  - uncertainty of the weights (from calibration certificate)
  - resolution of the device under test (DUT)
  - drift of the weight (calibration history)
  - repeatability (experiences)
  - temperature-coefficient DUT

# Calibration of rain gauges – example #1

- model:

$$\Delta_{\text{rain}} = \text{dut} - \text{reference} + \delta_{\text{dut\_resolution}} + \delta_{\text{dut\_repeatability}} + \delta_{\text{dut\_temperature\_coefficient}} - \delta_{\text{reference\_drift}}$$

$\Delta_{\text{rain}}$

dut

reference

result (dut - reference)

indication of dut intensity

indication of reference intensity

# Calibration of rain gauges – example #1

- uncertainties:

$\delta_{\text{dut\_resolution}}$

the resolution of the DUT is 0.01 mm

$\delta_{\text{dut\_repeatability}}$

the repeatability of the DUT is 0.01 mm

$\delta_{\text{dut\_temperature\_coefficient}}$

the temperature coefficient is 0.005 mm/K → maximum expected temperature change 1 K




$\delta_{\text{reference\_drift}}$

the estimated drift is less than 0.1 mg / 2 years



# Calibration of rain gauges – example #1

- result:  $\Delta_{\text{rain}} = -0.01 \text{ mm} \pm 0.01 \text{ mm} (k = 2)$

Quantity	Value	Stand. uncert.	Distribution	DoF	Sensit. coeff.	Uncert. contribution	Rel. contribution	Bar chart
dut	0,09 mm							
δdut_resolution	0,0 mm	0,00289 mm	Rectangular	∞	1,00 mm <sup>-1</sup>	0,00289	33,33 %	
δdut_repeatability	0,0 mm	0,00289 mm	Rectangular	∞	1,00 mm <sup>-1</sup>	0,00289	33,33 %	
δdut_temperature_coefficient	0,0 mm	0,00289 mm	Rectangular	∞	1,00 mm <sup>-1</sup>	0,00289	33,33 %	
reference	0,09996150 mm	6,00E-6 mm	Normal	∞	-1,00 mm <sup>-1</sup>	-6,00E-6	0,00 %	
δreference_drift	0,0 mm/min	2,89E-6 mm/min	Rectangular	∞	-1,00 min·mm <sup>-1</sup>	-2,89E-6	0,00 %	
	Value	Comb. stand. uncertainty	Effective degrees of freedom				Sign. digits	
Δrain	-0,00996	0,00500	∞				3	
	Value	Expanded uncertainty	Coverage factor (Probability)				Distribution	Sign. digits
Result	-0,010	± 0,010	2,00 (95,45 %)				Normal	2

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- Calibration example #1
- **Calibration example #2**

## Part 4:

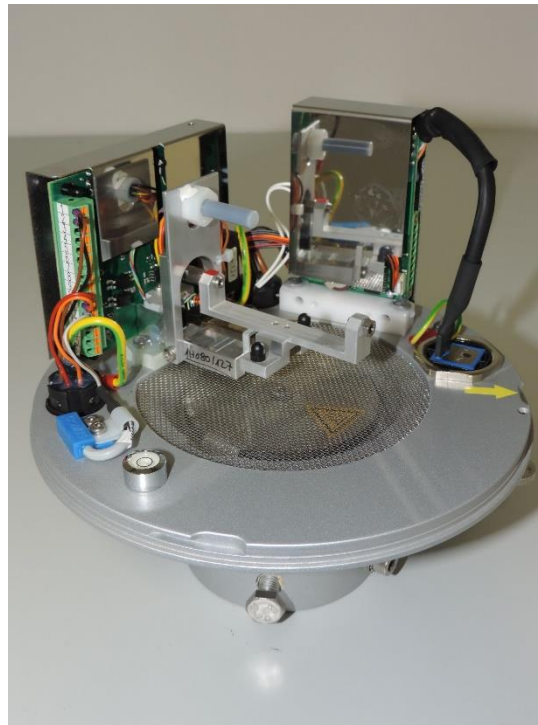
- Calibration example #3
- Calibration example #4
- References and links

# Calibration of rain gauges – example #2 (DWD)

- collecting rain gauge using a combination of tipping bucket and a weighing unit



assembled rain gauge



detailed view of the  
weight measuring unit



detailed view with installed  
tipping bucket

# Calibration of rain gauges – example #2

- the protective housing with the funnel is removed and the precipitation gauge is placed on a container made of PVC pipe
- this container is positioned on a precision balance together with the precipitation gauge
- instead of the original funnel, a replica of the funnel is positioned above the tipping bucket
- a pump whose speed can be varied to simulate the intensity of precipitation serves as a source

# Calibration of rain gauges – example #2

- the precision scale shall be placed on a very stable surface such as a measuring table with a granite plate (in this case a concrete platform was used)
- to avoid vibrations, the pump is decoupled from the measurement setup as much as possible
- the DUT is connected to the computer with a cable (USB, RS485 + power supply)
- this cable naturally influences the weighing but it has been demonstrated that the impact is nearly negligible compared to the total mass

# Calibration of rain gauges – example #2

- a stable room temperature is necessary
  - ⇒ if air conditioning is used, it shall be designed in such a way that draughts cannot influence the results of the precision balance (if necessary, the entire setup shall be shielded)
- a suitable equalization time must be provided to avoid temperature differences between the water and air temperature
- the water can be reused, but should be replaced with fresh water from time to time
- the precision balance shall be adjusted every day using calibrated reference weights

# Calibration of rain gauges – example #2

- the entire calibration process with three intensity levels (ten repetitions) is supported by a computer software
- the computer software controls the pump and reads the measured values from the device under test (DUT) and the precision balance
- the scale and the DUT are zeroed before each start of the pump

# Calibration of rain gauges – example #2

- it is essential that the air pressure, temperature and relative humidity are measured in a suitable place

```
TI33C3/SLN
00309564
PTB
20190729
10:17:49;1005.25
10:17:59;1005.25
10:18:09;1005.25
10:18:19;1005.25
```

air pressure data

```
TI33C3/SLN
00351871
HC2-USB
20190729
00:00:03; 19,18; 66,86
00:00:13; 19,15; 66,80
00:00:23; 19,16; 66,78
00:00:33; 19,14; 66,74
```

data of temperature and relative humidity

- the measured values are used to calculate the air density, the density of the water and thus to calculate the air *buoyancy correction*
- a precipitation amount is calculated from all these calculations and the measured value of the precision scale



# Calibration of rain gauges – example #2

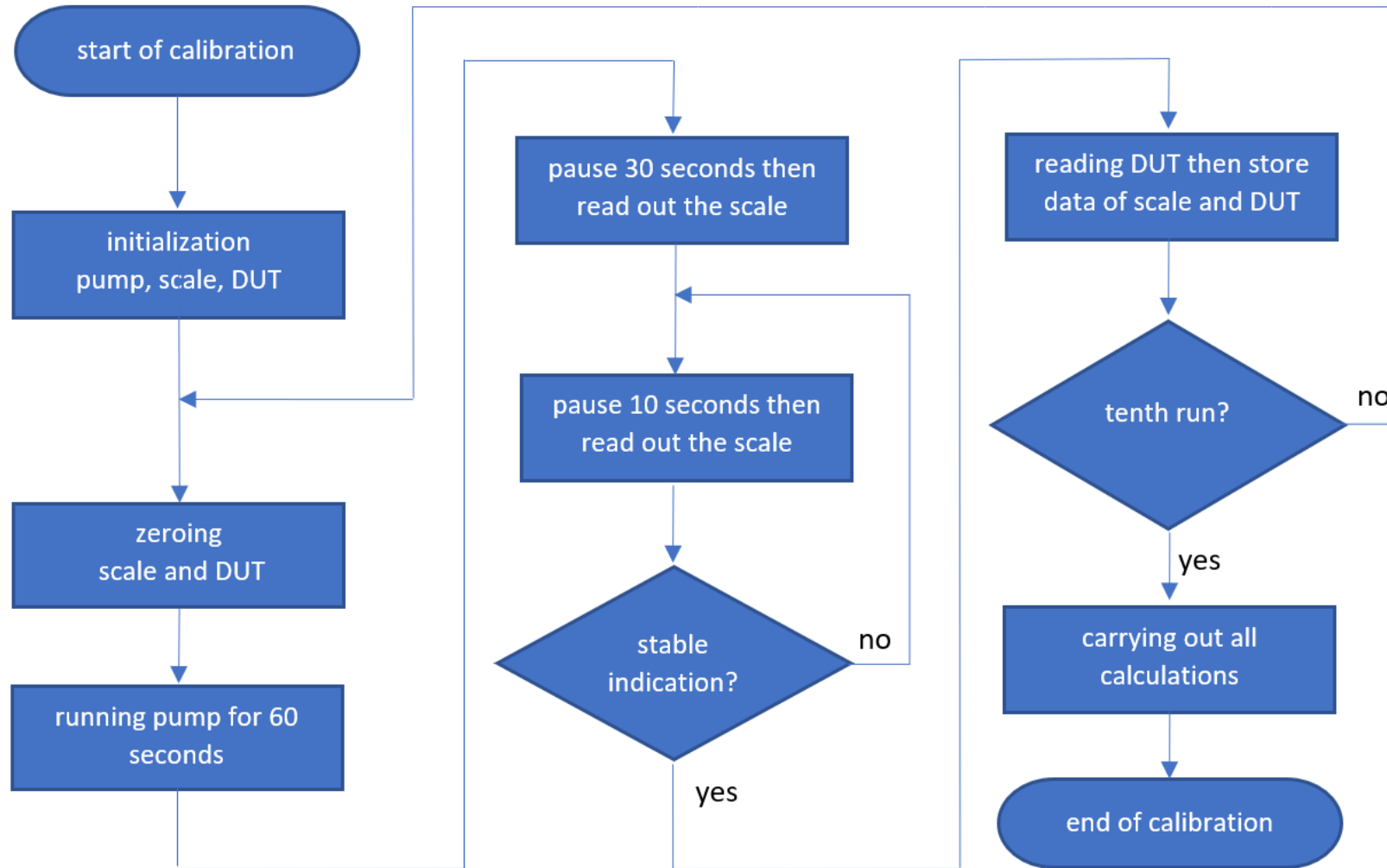


the complete calibration setup



detailed view

# Calibration of rain gauges – example #2



# Calibration of rain gauges – example #2

- it is assumed, that the water temperature is the same as the temperature of air with an uncertainty of 5 K (not very critical) → type B
- the uncertainty for the temperature of air is 2 K → type B
- the relative humidity uncertainty is 3 % → type B
- the air pressure uncertainty is 0.5 hPa → type B

# Calibration of rain gauges – example #2

- calculation of the amount in mm with modified formulas from EURAMET Calibration Guide No. 19 Version 3.0 (09/2018)

$$Q_{\text{water}} = 0.999974950 * (1 - ((t_{\text{water}} - 3.983035)^2 * (t_{\text{water}} + 301,797)) / \\ (522528,9 * (t_{\text{water}} + 69,34881))) + \\ (-4,612 * 10^6 + 0.106 * 10^6 * t_{\text{water}}) + \delta t_{\text{water}}$$

- note: All units are missing. Exact details in EURAMET CG 19 (1), (2)+(3), (5)!

# Calibration of rain gauges – example #2

- calculation of the amount in mm with modified formulas from EURAMET Calibration Guide No. 19 Version 3.0 (09/2018)

$$Q_{\text{air}} = ((0.34848 * p_{\text{air}} - 0.009 * u_{\text{air}} * \exp(0.061 * t_{\text{air}})) / (t_{\text{air}} + 273,15)) / 1000 + \delta t_{\text{air}} + \delta \text{air\_pressure} + \delta \text{relative\_humidity}$$

- note: All units are missing. Exact details in EURAMET CG 19 (1), (2)+(3), (5)!

## Calibration of rain gauges – example #2

- calculation of the amount in mm with modified formulas from EURAMET Calibration Guide No. 19 Version 3.0 (09/2018)

$$\begin{aligned} \text{reference\_in\_mm} = & (\text{reference\_indication\_g} * 1 / (\varrho_{\text{water}} - \varrho_{\text{air}}) * \\ & (1 - (\varrho_{\text{air}} / \varrho_{\text{reference\_weight}}))) / 20 + \\ & \delta_{\varrho_{\text{water}}} + \delta_{\varrho_{\text{air}}} \end{aligned}$$

- note: All units are missing. Exact details in EURAMET CG 19 (1), (2)+(3), (5)!

# Calibration of rain gauges – example #2

- model:

$$\begin{aligned}\Delta\text{rain} = & \text{dut} - \text{reference} + \delta\text{dut\_resolution} + \delta\text{dut\_splashed\_droplets} \\ & + \delta\text{dut\_evaporation} + \delta\text{dut\_emptying\_bucket} - \delta\text{cable\_influence} - \\ & \delta\text{reference\_evaporation} - \delta\text{reference\_resolution} - \delta\text{time}\end{aligned}$$

$\Delta\text{rain}$

dut

reference

result (dut - reference)

indication of DUT intensity

indication of reference intensity

# Calibration of rain gauges – example #2

- uncertainties:
  - type A: in this example there are ten readings of the precision scale and the DUT

reference_indication_g		dut
Name		
Method Direct		
No.	Estimated value	
1	0,99	
2	1,01	
3	1,02	
4	0,98	
5	0,97	
6	1,00	
7	0,99	
8	0,97	
9	1,02	
10	0,99	

dut_indication		reference_indication_g
Name		
Method Direct		
Unit g		
No.	Estimated value	
1	20,01	
2	19,99	
3	19,98	
4	20,02	
5	20,01	
6	19,98	
7	19,97	
8	19,96	
9	20,03	
10	20,04	

- the distribution is a t-distribution and the uncertainty estimation is Bayesian standard uncertainty



# Calibration of rain gauges – example #2

- uncertainties type B:

$\delta_{\text{dut\_resolution}}$

$\delta_{\text{dut\_splashed\_droplets}}$

$\delta_{\text{dut\_evaporation}}$

$\delta_{\text{dut\_emptying\_bucket}}$

$\delta_{\text{cable\_influence}}$

$\delta_{\text{reference\_evaporation}}$

$\delta_{\text{reference\_resolution}}$

the resolution of the DUT values is 0.001 mm

some droplets are splashed and do not end up in the bucket 0.0005 mm

evaporation may occur at DUT 0.00025 mm

during the tilting movement, water may still flow into the bucket to be emptied 0.005 mm

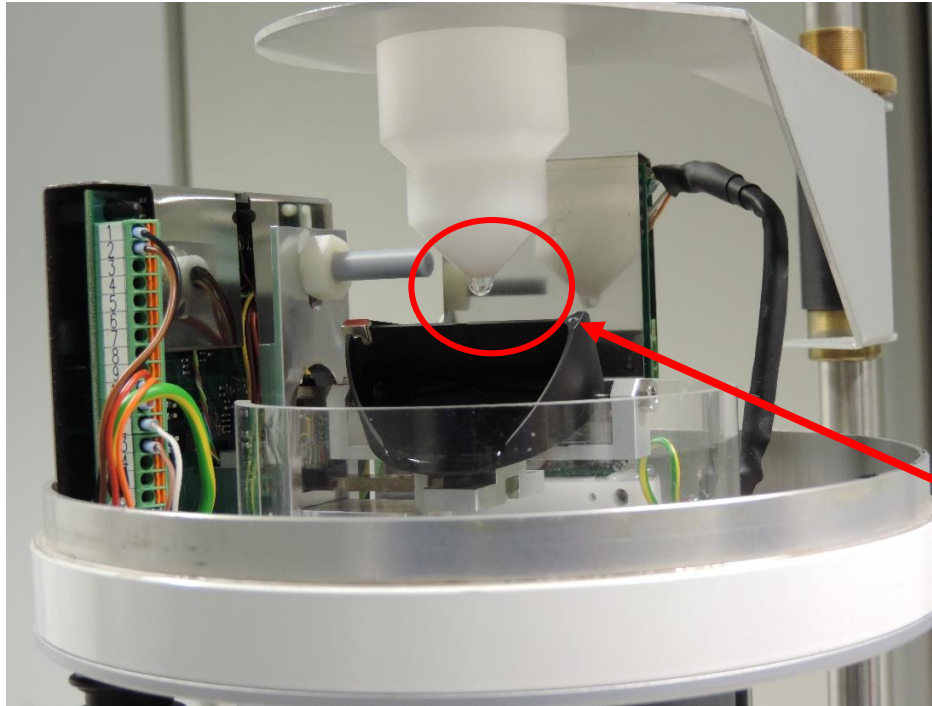
influence of the cable 0.001 mm

evaporation may occur at reference 0.00025 mm

resolution of the reference values are 0.00025 mm

# Calibration of rain gauges – example #2

- uncertainties:
  - $\delta\text{time}$



Will this drop fall?

# Calibration of rain gauges – example #2

- uncertainties:
  - $\delta\text{time}$ 
    - a residue of water can remain at the bottom of the funnel
    - this can fall down or get stuck depending on the dynamics and flow
    - experiments show that the mass of the falling drop can be as much as 0.14 g
    - the scale is read out first, then the DUT
      - $\Rightarrow$  the drop could fall between the two readings
  - observations show, however, that the event of a drop coming loose is extremely rare
  - in this uncertainty analysis, this contribution is taken into account with 0.2 g or 0.01 mm and a rectangular distribution

# Calibration of rain gauges – example #2

- result:  $\Delta_{\text{rain}} = -0.01 \text{ mm} \pm 0.02 \text{ mm} (k = 2)$

Quantity	Value	Stand. uncert.	Distribution	DoF	Sensit. coeff.	Uncert. contribution	Rel. contribution	Bar chart
$\rho_{\text{water}}$	0,99773 g/cm <sup>3</sup>	0,66x10 <sup>-3</sup> g/cm <sup>3</sup>						
$t_{\text{water}}$	22,2 °C	2,9 °C	Rectangular	$\infty$	-0,23x10 <sup>-3</sup> °C <sup>-1</sup>	-0,66x10 <sup>-3</sup>	0,58 %	
$\rho_{\text{air}}$	0,001208 g/cm <sup>3</sup>	0,012x10 <sup>-3</sup> g/cm <sup>3</sup>						
$p_{\text{air}}$	1,0268x10 <sup>3</sup> hPa	0,29 hPa	Rectangular	$\infty$	-1,0x10 <sup>-6</sup> hPa <sup>-1</sup>	-0,30x10 <sup>-6</sup>	0,00 %	
$u_{\text{air}}$	31,5 %rH	1,7 %rH	Rectangular	$\infty$	0,10x10 <sup>-6</sup> %rH <sup>-1</sup>	0,18x10 <sup>-6</sup>	0,00 %	
$t_{\text{air}}$	22,2 °C	2,9 °C	Rectangular	$\infty$	3,8x10 <sup>-6</sup> °C <sup>-1</sup>	0,011x10 <sup>-3</sup>	0,00 %	
reference	1,00329 mm	0,79x10 <sup>-3</sup> mm						
reference_indication_g	19,9990 g	0,0085 g	t-distribution	9	-0,050 g <sup>-1</sup>	-0,43x10 <sup>-3</sup>	0,24 %	
$\rho_{\text{reference\_weight}}$	8 g/cm <sup>3</sup>							
dut	0,9940 mm	0,0058 mm	t-distribution	9	1,0 mm <sup>-1</sup>	0,0058	44,08 %	
$\delta_{\text{dut\_resolution}}$	0,0 mm	0,29x10 <sup>-3</sup> mm	Rectangular	$\infty$	1,0 mm <sup>-1</sup>	0,29x10 <sup>-3</sup>	0,11 %	
$\delta_{\text{dut\_splashed\_droplets}}$	0,0 mm	0,29x10 <sup>-3</sup> mm	Rectangular	$\infty$	1,0 mm <sup>-1</sup>	0,29x10 <sup>-3</sup>	0,11 %	
$\delta_{\text{dut\_evaporation}}$	0,0 mm	0,14x10 <sup>-3</sup> mm	Rectangular	$\infty$	1,0 mm <sup>-1</sup>	0,14x10 <sup>-3</sup>	0,03 %	
$\delta_{\text{dut\_emptying\_bucket}}$	0,0 mm	0,0029 mm	Rectangular	$\infty$	1,0 mm <sup>-1</sup>	0,0029	10,87 %	
$\delta_{\text{cable\_influence}}$	0,0 mm	0,58x10 <sup>-3</sup> mm	Rectangular	$\infty$	1,0 mm <sup>-1</sup>	0,58x10 <sup>-3</sup>	0,43 %	
$\delta_{\text{reference\_evaporation}}$	0,0 mm	0,14x10 <sup>-3</sup> mm	Rectangular	$\infty$	1,0 mm <sup>-1</sup>	0,14x10 <sup>-3</sup>	0,03 %	
$\delta_{\text{reference\_resolution}}$	0,0 mm	0,14x10 <sup>-3</sup> mm	Rectangular	$\infty$	1,0 mm <sup>-1</sup>	0,14x10 <sup>-3</sup>	0,03 %	
$\delta_{\text{time}}$	0,0 mm	0,0058 mm	Rectangular	$\infty$	1,0 mm <sup>-1</sup>	0,0058	43,50 %	
$\Delta_{\text{rain}}$	-0,0093	Comb. stand. uncertainty 0,0088	Effective degrees of freedom 46		Sign. digits 2			
Result	-0,01	Expanded uncertainty $\pm 0,02$	Coverage factor (Probability) 2,00 (95,45 %)		Distribution Normal		Sign. digits 1	

## Calibration of Rain Gauges End of Part 3

# Thank you.



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